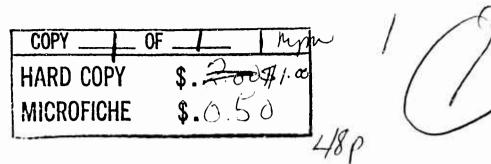


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SC-RR-64-979

THE HYPERSONIC PLASMA CONVERTER: IF

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November 1964

ABSTRACT

As a continuation to Part I—of the hypersonic plasma generator known as ASP (Aerodynamic Supply of Power), experimental analyses have been extended to investigate in detail the various parameters that govern the operation of the generator. A final feasibility study was made, and possible modifications to the theory are outlined. Test runs in the Sandia Corporation are jet with air as the working fluid at 12,000 BTU/lb have generated 8 amp/in 2 short circuit currents and 2, 3 volts open circuit voltage. Under favorable conditions, full-size re-entry vehicles in the altitude range of 200,000 to 80,000 feet are expected to yield several kilowatts of power.

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LIST OF SYMBOLS

```
A<sub>e</sub>(ox A<sub>em</sub>) - emitter area
```

A_c - collector area

 $C - aRI_{th}/(\sigma V_T)$

D - diffusion coefficient

E - emf or electric field (volts)

e - electronic charge 1,60207 x 10^{-19} coulombs

h - Planck's constant

I - current (amperes)

 $i - I/I_{th}$

isc - Isc/Ith (short circuit current)

 $_{\rm J}, {
m J}$ - current density, ${
m amps/in}^2$

k - Boltzmann constant 1,3709 x 10⁻¹⁶ erg/deg

L - characteristic length

 $m_{\mbox{\scriptsize e}}^{}$, $m_{\mbox{\scriptsize i}}^{}$ - electronic and ionic mass, respectively

P - power (watts)

p - pressure

R - emitter radius

r - resistance

 r_p, r_c, r_L - plasma, contact, and load resistance, respectively

T_e - electron temperature

T_{em} - emitter surface temperature

T - collector surface temperature

v - velocity

V - potential (volts)

 V_{oc} - open circuit potential

 ${f V}_{f T}$ - plasm i temperature equivalent potential

LIST OF SYMBOLS (cont)

 $v_{T_{em}}$ - emitter temperature equivalent potential

 $V_{\mbox{em}}$ - emitter sheath potential

V - collector sheath potential

Greek Symbols

 α - a fraction in definition of C

$$\beta - I_{\text{eem}}/I_{\text{ec}} \sim A_{\text{em}}/A_{\text{c}}$$

$$\gamma$$
 - $I_{ic}/I_{ec} \simeq 1/155$ for air

 ϵ - dielectric constant

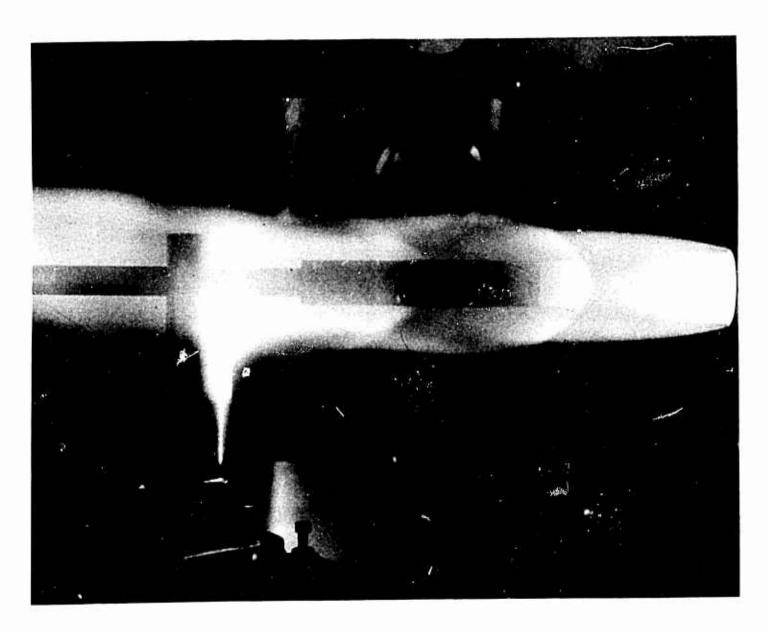
 θ - spherical coordinate (in Appendix θ = $kT_{\underline{e}}/e)$

 μ - mobility

 σ - electrical conductivity mhos/cm

au - time

 $\emptyset_{e,c}$ - work function (in Appendix B and C, \emptyset = potential)



Frontispiece. A Hypersonic Plasma Generator

THE HYPERSONIC PLASMA CONVERTER

Introduction

The operational principle of the hypersonic plasma generator has been discussed in detail in Part 1 (Reference 1) of this two-part report. Briefly, the nose cone of a re-entry vehicle serves as a thermionic emitter of electrons, or a cathode (see Figure 1). These electrons are then conducted through the shock ionized stream, increased in kinetic energy by collisions, and collected over the relatively cool vehicle afterbody which is electrically insulated from the nose cone and which serves as an anode, or a collector. A load connected between the cathode and the anode within the vehicle completes the circuit. The generator has the basic features of a plasma thermocouple and, for its power output depends primarily on the large temperature and area differences between emitter and collector, with the kinetic energy of the plasma electrons as its energy source.

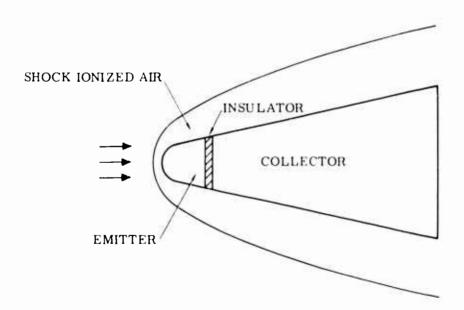


Figure 1. Schematic of ASP Generator

In addition to the several references mentioned in Reference 1, two more works (References 2 and 3) have been published recently which deal with the ASP generator. The first work summarizes the righ points of both Reference 1 and the present report. The second work summarizes the progress reports of the work done by the Electrical Engineering Department of the University of New Mexico on a contract with Sanda. Corporation starting January 1963 and ending June 1954.

Theory

For a full treatment of the theory of the plasma generator the reader is referred to Reference 1 and several references quoted therein. We repeat briefly the salient points in its development, the space-charge neutralized volt-ampere characteristics ($V_{\rm em} < 0$, $V_{\rm em}$ -emitter sheath potential) of the generator can be represented by Equation 5 from Reference 1, or,

$$V = \left(\frac{kT_{e}}{e}\right) In \left[\frac{I_{ec}}{I_{eem}} \left(\frac{I_{th} + I_{tem} - I}{I_{tc} + I}\right)\right] + (\emptyset_{e} - \emptyset_{c}) - Ir$$
(1)

where

T_e - electron temperature

 $I_{\stackrel{\scriptstyle }{e^{\, }c}}$ - random electron current to collector

 $I_{\stackrel{\cdot}{\mathrm{eem}}}$ - random electron current to emitter

 I_{th} - thermionic emission current

 $I_{\stackrel{\cdot}{\text{lem}}}$ - random ion current to emitter

 I_{ic} - random ion current to collector

 ϕ_c , ϕ_c - work functions of emitter and collector respectively

 $\mathbf{r}(\mathbf{r}_{p},\mathbf{r}_{c},\mathbf{r}_{t})$ - circuit resistance (plasma, contact and load)

The open circuit voltage then becomes

$$V_{\text{OC}} = V_{\text{T}} \left[\ln \left[\frac{1}{\beta} \left(\frac{1 + \gamma/\delta}{\gamma/\delta \beta} \right) \right] + \emptyset_{\text{C}} - \emptyset_{\text{C}}$$
 (2)

where, there has been regroduced the notation of Waymouth, Reference 4, or

$$\beta$$
 I_{eem} I_{ec}

$$\gamma = I_{1C}/I_{eC}$$

$$\delta = I_{th}/I_{eem}$$

 $\mathbf{V_{T}}$ = voltage equivalent of plasma electron temperature

For $V_{em} > 0$ (e.g. $\delta \sim 1$), Equation 2 changes to

$$V_{\text{oc}} = V_{\text{Term}} \ln \delta / \gamma + V_{\text{t}} \ln 1 / \gamma + \emptyset_{\text{c}} - \emptyset_{\text{c}}$$
(3)

where V_{Tem} - voltage equivalent of emitter temperature.

The short circuit current, on the other hand, follows by setting $V = \Delta \emptyset = 0$

$$I_{SC} r = V_T I_0 \left[\frac{1 + \gamma/\delta - I_{SC}}{\gamma/\delta + \beta I_{SC}} \right]$$
(4)

where

$$r_{\rm sc}$$
 - nondimensional current $I_{\rm sc}/I_{\rm th}$.

For zero resistance, Equation 4 can be simplified to yield (Reference 4)

$$I_{SC} = \frac{I_{th}}{1 + \beta} \tag{5}$$

or, if back emission from the collector I_{th}^{i} is included

$$I_{sc} = (I_{th} - I_{th}^{\dagger} \beta)/(1 + \beta)$$
 (6)

It should be noted that the basic volt-ampere characteristics equation above has been derived on the basis of a rather unrealistic assumption of constant electron temperature around the vehicle and a constant electron density. As will be shown later, the gas temperature in the flow field changes approximately 40 degrees while expanding over a 12-degree hemisphere cone. Electron densities can decrease by as much as three orders of magnitude from emitter to collector. Furthermore, because of large currents (20-30 amps/in²) being dumped in the plasma jet, joule heating and Thompson effects may become prominent in disturbing the plasma temperature distribution. These and other modifications necessary for refining the ASP generator theory are discussed in detail in the Appendix.

Experiments

To verify the analytical predictions of the hypersonic generator, an extensive set of experiments were performed in the Sandia Corporation 160 kw plasma arc tungel. The various model geometries used in the plasma tunnels are shown in Figure 2.

A. Test Conditions

The average diameter of the models and of the plasma jet was 3/4 inch and 1-1/4 inches, respectively. The details of the flow field around an S-6 model in the 160 kw plasma jet, with argon and air as the working gases are presented graphically in Figures 3 through 7 and tabulated in Tables I and II. As observed from this data, the average flow Mach number is 2,5-3,0 with mean energy inputs to the jet of 5000 BTU/lb for argon and 12,000 BTU/lb for air (or nitrogen). The ambient pressure in the test chamber is of the order of 7 mm (-0.01 atm) and stagnation pressures range from 0.06 to 0.13 atm. Figure 7 shows the equilibrium and nonequilibrium calculations of the temperature in the jet for air at various energy inputs over a

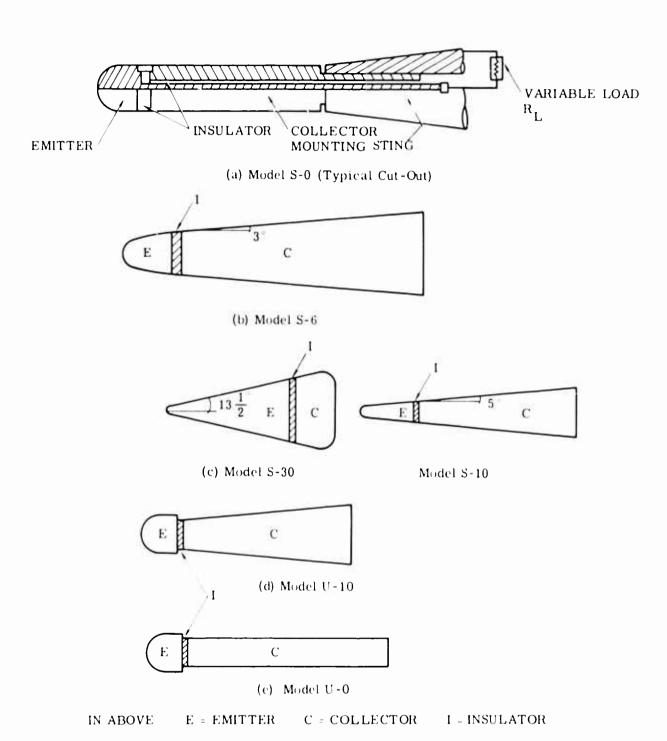


Figure 2 Sketches of ASP Plasma Jet Models

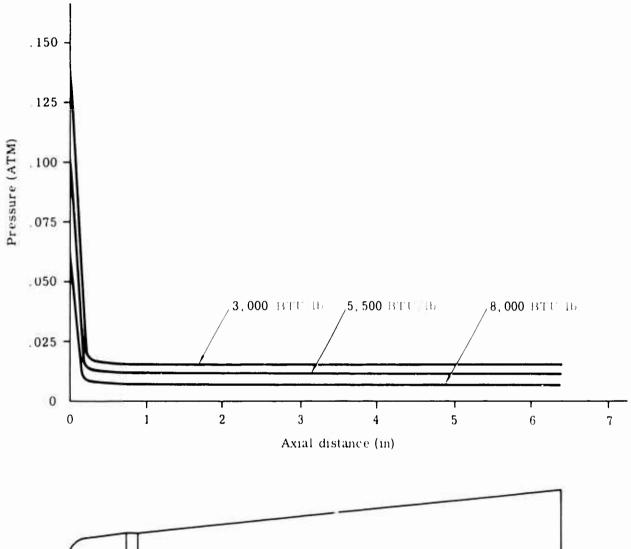


Figure 3. Surface Pressure on S-6 Model in 160 kw Jet (Argon)

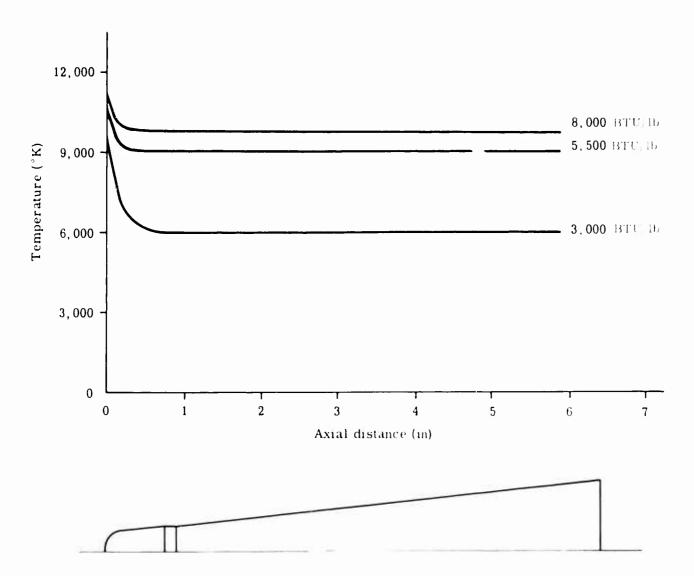


Figure 4. Kinetic Temperature Neur Bod, of See Model at 150 kw der (Vigon)

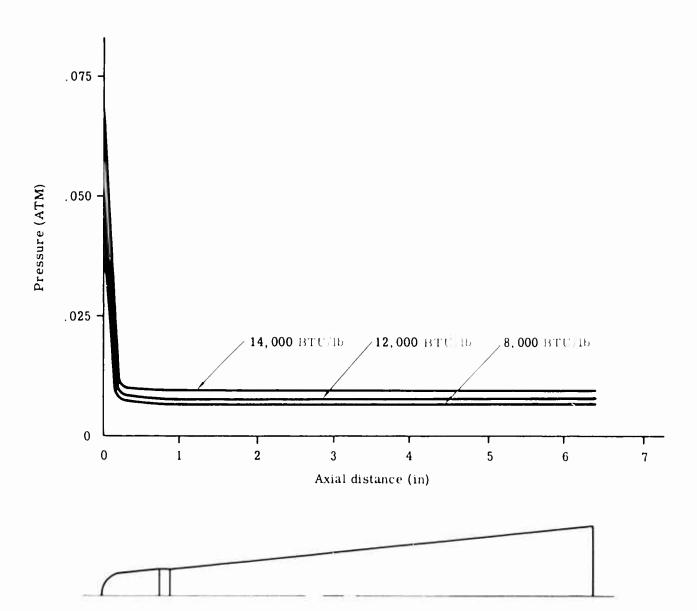


Figure 5. Surface Pressure on S-6 Model in 160 kw Jet (Air)

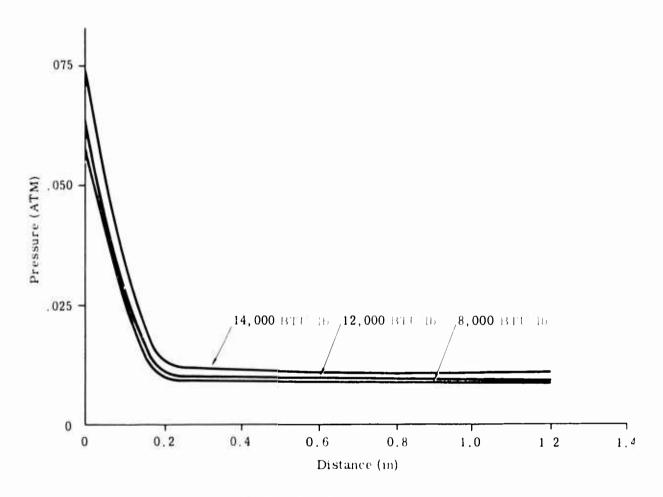


Figure 6. Surface Pressure on S-6 Model in 160 kw let (Air Nose Cone Section Enlarged)

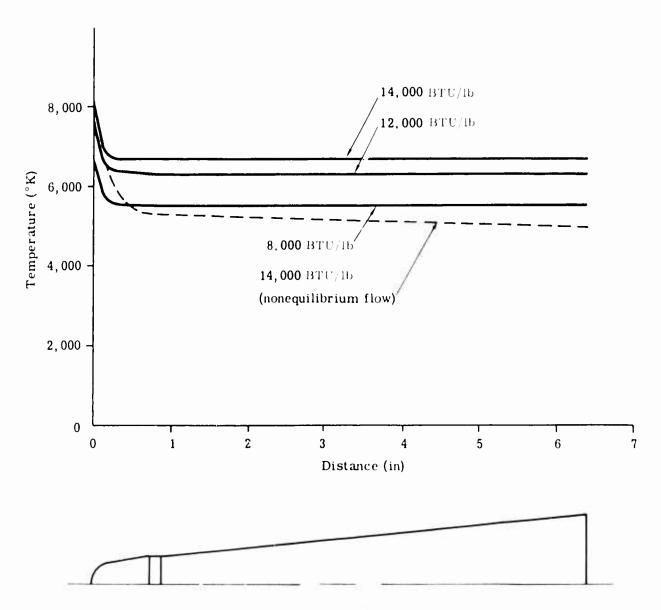


Figure 7. Kinetic Temperature Near Body Surface of S-6 Model in 160 kw Jet (Air)

TABLE I

Electron Density in Argon Gas

Distance (Axial)	n _e	n	ne/n		
	3000	BTU/lb			
0	0.2×10^{15}	10 ¹⁷	6.2×10^{-2}		
0, 125	5.2×10^{14}	3, 75 x 10 ¹⁶	1.39×10^{-2}		
0, 207	3.7×10^{13}	1.78×10^{16}	2.08×10^{-3}		
0.750	3, 75 x 10^{12}	1, 77 x 10 ¹⁶	2.12×10^{-4}		
	5500	BTU/lb			
0	8.35×10^{15}	6.8×10^{16}	1.23×10^{-1}		
0, 125	5, 5 x 10 ¹⁵	2.02×10^{16}	2.7×10^{-1}		
0,210	6.3×10^{14}	1.06×10^{16}	5.95×10^{-2}		
0.750	5.5×10^{14}	9.00×10^{15}	6.1×10^{-2}		
$8000~\mathrm{BTU/lb}$					
0	1.15 x 10 ¹⁵	3.9×10^{16}	2.95×10^{-1}		
0, 125	3, 05 \times 10 ¹⁵	1.4 \times 10 16	2.16×10^{-1}		
0.207	3.0×10^{15}	5,8 \times 10 15	5.19×10^{-1}		
0.750	1015	$5, 2 \times 10^{15}$	1.92×10^{-1}		

TABLE II

Electron Density in Air

Distance (Axial)	n _e	n	ne/n		
	8,000	BTU/lb			
0	6.15 x 10 ¹³	6.4×10^{16}	9.6×10^{-4}		
0.125	9.25×10^{12}	2.5×10^{16}	3.7×10^{-4}		
0.207	$3,48 \times 10^{12}$	1. 25 \times 10 16	2.8×10^{-4}		
0.750	3,08 x 10 ¹²	1, 14 \times 10 ¹⁶	2.7×10^{-4}		
	12,000	о вти/њ			
0	2.58×10^{14}	6.0 x 10 ¹⁶	4.3×10^{-3}		
0, 125	5.03 x 10 ¹³	2.35×10^{16}	2.1×10^{-3}		
0.207	1.43×10^{13}	1, 20 \times 10 ¹⁶	1.2×10^{-3}		
0.750	1, 16 x 10 ¹³	1.08 \times 10 ¹⁶	1.07×10^{-3}		
14,000 BTU/lb					
0	6.05×10^{14}	6.8 x 10 ¹⁶	8.9×10^{-3}		
0, 125	1.07 \times 10 ¹⁴	2.7×10^{16}	4.0×10^{-3}		
0.207	3.05×10^{13}	1, 35 \times 10 ¹⁶	2.3×10^{-3}		
0.750	$2,66 \times 10^{13}$	1.24×10^{16}	2.2×10^{-3}		

blunted cone (12-degree included angle) model. Kinetic temperatures are seen to fall by 40 percent for low-energy inputs and 25 percent for high-energy inputs in the equilibrium-flow calculations. These values are high by about 15-20 percent when they are compared to more realistic nonequilibrium calculations. Some of the latter were extrapolated directly from TRW/STL Laboratories, using calculations applied to prototype flight conditions (see Figure 8). Corresponding drops in ionization levels are given in Tables I and II.

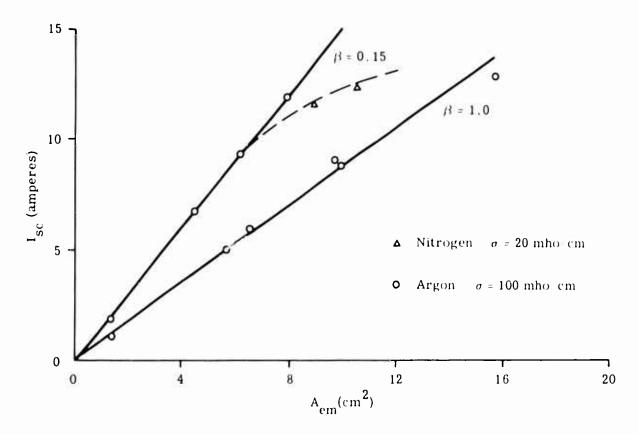


Figure 8. Short-Circu: Carrent Versus Emitter Area for Two Values of Effective , (... Runs made in Argon Gas with 5000 BTU lb Energy, and Nitrogen at 12,600 BTU/lb.

B. Parameters Influencing Generator Output

The detailed theoretical analyses made in References 1_{\circ} 4, and 5 and in the Appendix of this reportation as set of parameters that govern the output of the plasma generator independently and or collectively. These may be listed as follows:

1. Emitter Area -- (χ_{em}) is directly proportional to the thermicene class ion rate in the Riemardson-Dushman formula

$$I_{\text{th}} = (\text{constant}) A_{\text{cm}} T^2 \exp \left(-\frac{\epsilon \emptyset}{kT_{\text{cm}}}\right)$$

and hence determines the magnitude of short circuit current output according to Equation 5

- 2. Emitter to Collector Area Ratio -- ($\beta \approx \Lambda_{\rm em}/\Lambda_{\rm c}$) is proportional to the ratio of random electron current at the emitter to that at the collector. In Equation 2 this parameter acts like a resistance
- 3. Emitter and Collector Surface Temperatures -- ($T_{\rm em}$, $T_{\rm e}$) electron emission is directly proportional to surface temperature according to the Richardson-Dushman equation above. From Equation 6, one can note that $T_{\rm em} \gg 3$ for minimum back emission.
- 4(a). Kinetic Temperature in Plasma -- (T_e) is the very source of the generator energy. Equations 2 and 3 show the open circuit voltage to be directly proportional to the electron temperature T_e and to depend logarithmically on the degree of ionization in the plasma which is also a direct function of T_e .
- 4(b) Degree of Ionization (n n) determines the power output directly through the term of quation 2) and indirectly by neutralizing the space charge created by the emission electron cloud at the cathode. It is proportional to the gas pressure and temperature.
- 4(c). Plasma Resistance -- (r) limits the effective length of the collector and consequently has a direct bearing on reducing the increased short circuit current output brought about by an increase in vehicle size, e.g., $\frac{\lambda_{em}}{2}$
- 5. Contact or Internal Resistance -- Either resistance is a significant constituent to the total generator internal impedance for the plasma jet scale models. It occurs primarily at the collector-to-sting contact point (see Figure 2a).
- 6. Emitter and Collector Material -- These govern the output through two factors—the work function, which in turn governs the electron emission rate and under proper conditions can supply as $\min(1.48,1.5)$ volts through $\emptyset_{e}^{-} = \emptyset_{e}^{-}$ in Equation 1, and the electrical properties which contribute to the total internal impedance of the generator. Because the ASP is a low--oltage, high-current device, the internal impedance should be kept minimal.

It is obvious that there is a strong interdependence among the various parameters listed above. For example, a favorable effect expected by a change in one parameter might cause an adverse effect on another. The following experimental results show these various effects, and with the theoretical predictions, can lead one to establish optimum working conditions for the hypersonic plasma generator.

C. Experimental Results

The results reported here were collected during a year in Sandia Corporation's 160 km plasma jet facility. Final experiments are now under way in the 1-mm facility with larger models to study in greater detail the effects of parameters 1 and 2.

1. Emitter Area -- Table III lists the various sizes of emitters and collectors used. The emitter areas vary between 0.8 and 2.50 m² and β varies between 1 and 0.08. As predicted from Equation 5, the short circuit current shows a linear dependence of $\Gamma_{\rm SC}$ on the emitter area (Figure 8). According to Equation 4, this linear dependence should change as the plasma resistance becomes significant ($\Gamma_{\rm p} + 0.01\,{\rm ohm}$). This effect was noticed clearly in mitrogen, but was insignificant in argon because of the high degree of ionization in the latter. Because of the limited size of the jet and consequently of the models, only "trends" were obtained in nitrogen gas represented by the dotted lines in Figure 8. The open-circuit voltage showed no dependence on the emitter area as predicted from Equation 2. Figure 9 compares outputs from two geometrically similar models with different emitter areas.

TABLE III

Model Dimensions

	Emitter Area	Collector Area			
Model	(in ²)	(in ²)			
S-0	0.85	5, 89			
and	1, 70	9, 82			
U-0	1,03)	9, 82			
	$\left. \frac{1,03}{1,18} \right\}$ Pyrographite	9, 82			
U-10	Same	9, 95			
S-10	0, 70	4, 95			
S 30	0, 86	0, 84			
	2, 48	2, 44			
S-6	1.30	16,60			

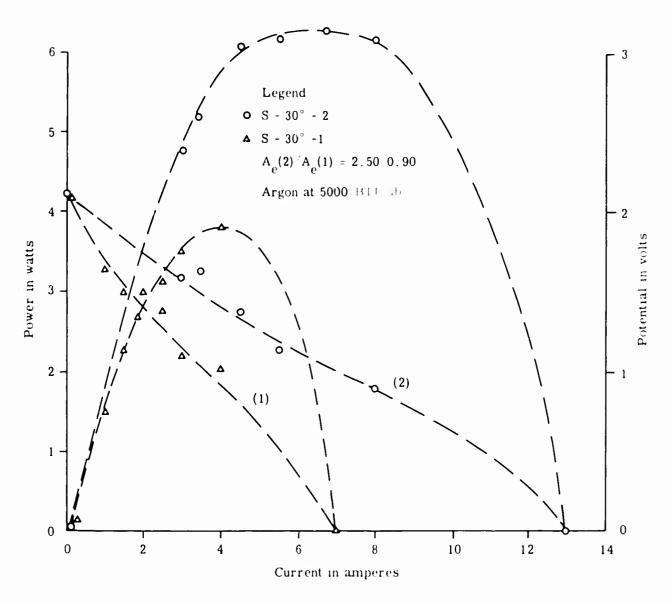


Figure 9. Output from Geometrically Similar Models with Different Finitter Areas

- 2. Emitter to Collector Area Ratio -- A large number of runs were made to determine the effect of β on power output, especially on the short-circuit current. Figure 8 shows this effect graphically. In general, the trend follows theoretical predictions, however, for most models the effect of flow separation over the model afterbody, the contact resistance between sting and collector (see Figure 2a), and the plasma resistance becoming effective for $\beta \geqslant 0,2$, could not be identified separately and, consequently, an effective $\beta \triangleq \beta^{\dagger}$ was used to correlate data. For negligible r_p and r_e , the data fit the curve i * $1/4 th^{\frac{1}{2}} 1/(1+\beta)$ best for "wetted" collector areas only. These were determined visually by observing detachment and reattachment points and collector surface glow. For increasing plasma resistance (e.g., air and introgen runs) the points on $1/8 th^{\frac{1}{2}} th$
- 3. Emitter and Collector Surface Temperature -- These temperatures were measured with a two-color pyrometer attached to a recording chart. When the arc jet glow overshadowed surface color temperatures, the jet was turned off instantaneously and the surface temperature estimated from the time-temperature decay history, with an accuracy within $\pm 100^{\circ}$ C. Depending on the arc jet energy and model material, average values of $T_{\rm em}$ varied between 2300 and 3200°C. Stagnation point temperatures exceeded 3400°C on sharp cone models (Figure 2c). This temperature was deduced from observing melting tungsten. $T_{\rm c}$ was less than 1200° C for S-0 models (see Figure 2), about 1500° C for model S-6 surfaces, and 1800° C for S-30 models. Back emission from the collector becomes signific and for $T_{\rm c}^{-1}T_{\rm em} \ge 0.8$. Maximum tested cone angles were 30° with $T_{\rm c}^{-1}T_{\rm em} \le 0.7$. Figure 10 shows the output for four geometries having comparable $\Delta_{\rm c}^{-1}(1+\beta)$. Hammerhead geometries are shown to reduce output because of reduced effective β arising from flow separation. $\Delta_{\rm c}^{-1}(1+\beta)$ for S-30 was twice that of S-10 with a slightly lower output, probably because of considerable back emission from the S-30 and very large $\beta(\beta=1,0)$.
- 4(a). Kinetic Temperature in Plasma -- Accurate estimates of this parameter were difficult to make. Calorimetric and pitot pressure studies (Reference 6) combined with spectrographic estimates (Reference 7) gave values of 12,000 $^{\circ}$ K electron temperatures at the stagnation point of the ASP vehicle in 5000 BTU 1b argon gas. In air, stagnation temperatures were estimated at 7500 $^{\circ}$ K for 12,000 BTU/1b energy input Unfortunately, no spectrographic results are available at present to check this magnitude which may be somewhat optimistic. Figure 7 gives plots of T_e over an S-6 shape model for air, using both equilibrium and nonequilibrium reaction calculations. The maximum temperature drop from stagnation point to afterbody is of the order $T_0 T_0 \simeq 0.5$.

To estimate open-circuit voltage values under optimum run conditions, which in argon would correspond to $V_{\rm T}=1~{\rm ev}$, γ = 1/293, and in air $V_{\rm T}$ = 0.7 eV, γ = 1/155, the following table is obtained:

TABLE IV

Open-Circuit Voltage

	Argon		/11		
	8	V (volts)	8	V (volts)	
$V_{em} \subseteq 0$	0.10	3, 42	0.10	1, 92	
(Eq. 2)	0, 01	i, 37	0.01	0.67	
V _{em} · 0	0.10	6, 51	0.10	4, 22	
(Eq. 3)	J. 01	5, 95	0.01	2.03	

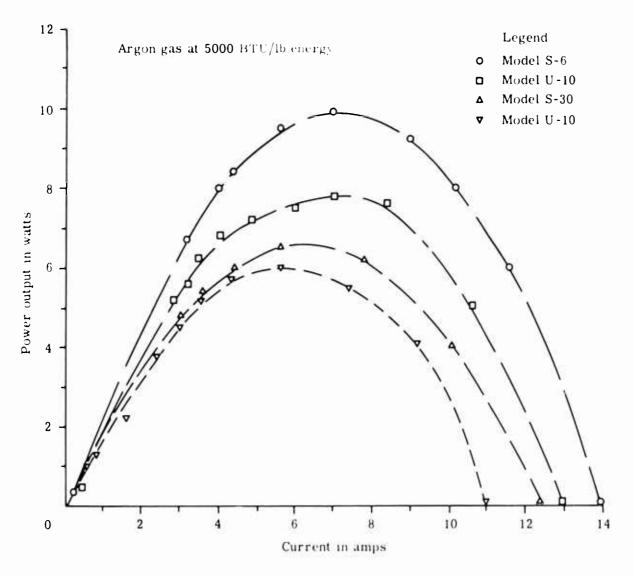


Figure 10. Power Output for Various Model Geometries at Constant let Fierry.

Measured values in argon averaged about 3.3 volts with the exception of a value of 4.45 volts registered with model tip flush with nozzle exit where $V_{\rm T}$ might have been closer to 4.3 ev (1 ev stagnation point temperatures were measured at a point 1 inch downstream of nozzle exit where most of the tests were run). This indicates that the emitter sheath $V_{\rm em}$ was possibly negative. A note of caution, however. Equations 2 and 3 are based on the assumption $T_{\rm e}$ is the same at both emitter and collector. For $T_{\rm ec} = 0.7$ $T_{\rm em}$ it is possible to obtain 4 volts open-circuit voltage with $V_{\rm em} = 0$ and $\delta = 0.1$ see Appendix). Corresponding measurements in air gave optimum values of 1.9 to 2.3 volts open circuit.

4(b). Degree of Iomization -- From above values of $T_{\rm el}$ (Tables I and II), the percent ionization in the gas around the ASP model can be summed up. In section 4(a) above values of γ were based on complete charge neutralized flow conditions. This, however, was not the case for all test conditions, as was evident from special seeded gas runs where values of $V_{\rm oc}$ increased by 15 to 25 percent, depending on energy input, and $I_{\rm el}$ by as much as 100 percent (see Table V below).

TABLE V

Output with and without Seeding

		So Seed		1^r K_2CO_3 Added	
Cins	Energy BTU 1b	\ () ₍	Isc	Λ,	Isc
Argon	5,000	1.2	14.0	2. 2	18.0
	4,500	2.5	10.0		15, 0
Nitrogen	14, 000	1, 15	4. ()	1,55	7, 5
	12,000	1.20	3, 0	1.70	6, 4

Two types of seed material were used, KCl and K_2CO_3 . Because of the electronegative properties of KCl where $V_{\rm OC}$ -seeded gave 10 percent lower values than $V_{\rm OC}$ -no seed, the KCl was discarded. K_2CO_3 powder was fed downstream of the arc at the rate of 1 gm/min, or a maximum of 1 percent by weight of the gas mass flow. The effect of ionization on short-circuit current output is further illustrated in Figures 11 and 12 where, in addition to seeding, special runs are shown which were made with various mass ratios of $A\text{-}N_2$ gas. Figure 13, on the other hand, compares runs in argon, air and nitrogen on the same model and comparable energy inputs, with maximum output decreasing from 13 watts to 3 watts, respectively.

40.). Plasma Resistance r -- Referring to Equation 4, the short-circuit current is seen to depend on the plasma resistance through the term r. If one assumes r to be represented by

$$r = 1$$
. σ

$$=\frac{aR}{\sigma}$$

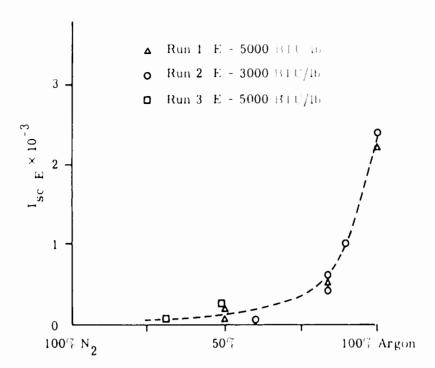


Figure 11. Degree of Conzation on Short Care at Current Output, Aigon-Nitrogen Mixtures

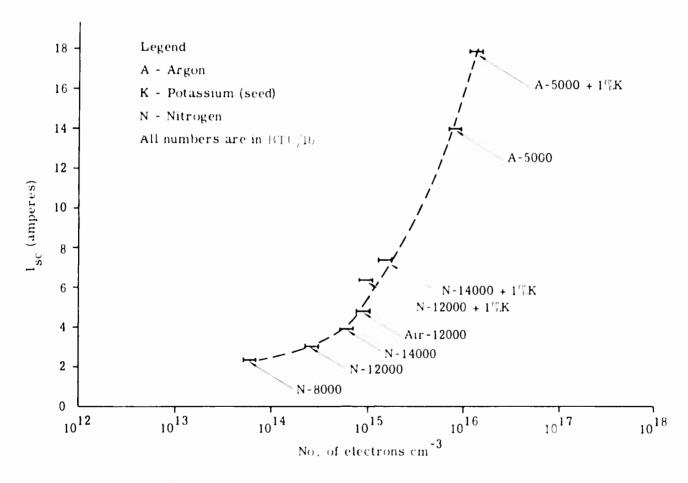
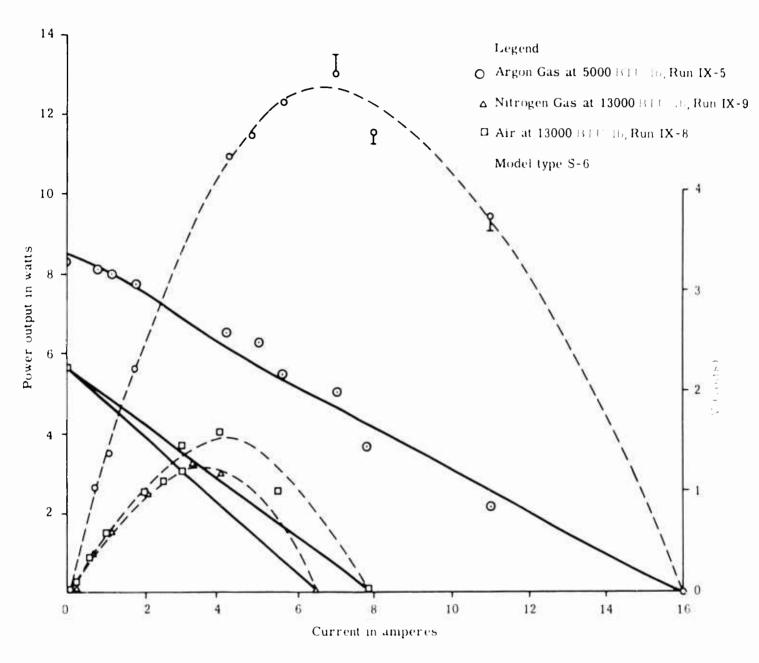


Figure 12. Short Circuit Current versus Electron Densits (Unseeded Gas from Spectroscops, Seeded Gas Using Saha aquation)



Lighte 15. Power Output and V-I Characteristics of 8-6 Model in Argon, Nitroger and Air

A 1 + 1 +

R : emitter ridges (cm)

plasma conductivity inhos cm

c some Traction less than one, depending on trajectory

I saction 4 can be rewritten

$$C_{1} = I_{0} \left[\frac{1 + \gamma \cdot \delta - i_{S_{0}}}{\gamma_{1} \cdot \delta + \beta i_{S_{0}}} \right]$$
 (7)

where $C = a \operatorname{RL}_{ch} \sigma \nabla_{\Gamma}$. Equations 5 and 7 are plotted in Figure 14. It is clearly seen that, for a given β the short circuit current falls below the r=0 (or $\sigma \to r$) value if plasma resistance is included. The For stant resistance curves show a significant reduction in short circuit current for Figure B . In fact, π small β in a low plasma conductivity or larger electron trajectory (cR) is discless as seen from $\alpha \beta$. $\epsilon=10$ For $\gamma=1$ 155 the curves in Figure 14 lie about 5 percent below the $\gamma=1$ 293 curves. From sections 4(a) and 4(b) σ in argon was estimated as 100 mho cm and plant as 20 mho cm. For a 10 cm. effective electron trajectory this corresponds to $\frac{1}{2}=0.1$ ohm, and 0.4 ohm, respectively. If one compares the r_{SC} output in argon and in air for a given B and R_{CTS} (argon) $\pm 2 r_{SC}$ (air). This difference is believed to result partially from reduced thermionic emassion in air as compared to argon because of possible lack of charge meatralization in the former (ionization in argon is a factor of 10 greater than in air), and partialls $\text{for example for } R=1\text{ cm, } \alpha=0.2\text{ I}_{11}\text{ (argon)}-2\text{ (I_{12}\text{ arr})}-\sigma_{\chi}-100-\sigma_{\text{arr}}=20,\ \chi_{\overline{\chi}}=1.0$ 1 0 7 then Cargon Cair 0 23 Answ set of experiments presently under was in the Sandia Plasma Laboratory 1 mw tacility with model sizes 2 to 10 times longer than those used in the 160 kw too life will enable us to determine this effect with greater accuracy (see helow). Several mins with insulator lengths varying between 0-2 to 2-0 inches in argon indicated no significant changes n , $\frac{1}{8n}$ output. In mirrogen on the other hand, there was observed a 15 percent reduction in . Twhen insulator length with increased from 0.25 inch to 1.5 inches for a fixed contact resistance r

omitter and the pick-up rod and between the collector and the starg writers appointed the model and served as the connector for carrying current to external load. These tables were minamized by using cadmium solder which melted upon heating and made a liquid contact, or, TP-Hg-In liquid metal allow it the two contact points. Minimum values of r were of order 0.1 ohm and often as high as 0.5 ohm. Maximum power output generally occurred at r = 0.2 ohm, indicating a possible r + r = 0.2 ohm index conditions of optimum internal impedance control. Much more reliable values are forthcoming in the Targe scale-model tests now indexway in the 1 mw facility.

Figure 14. Dimensionless Short-Careal Careal Gersus I B for Various Resistance Farancetes Cana Argon and at An

6. Materials -- Table VI lists the type of materials used as emitters, insulators, and collectors,

TABLE VI

Model Materials

Limitter	ntter Collector	
VIJ graphite	ATJ graphite	Boron nitride
Pyrolitic graphite	Pyrolitic graphite	$A1_2O_3 = 99, 6\%$
Phenolic carbon	Phenolic carbon	99, 8"
Tungsten	Tungsten	BMI 785*
Tantalum	Tantalum	$1_{9}O_{3} + 5$ volume
Zirconium-carbide +	Niobium	percent Mo
graphite, eutectic	Molybdenum	
	Cb - 10, W-2, 5, Zr	$M_2O_3 \cdot \beta$ volume
	Ta - 10 W	percent W
	Mo - 0, 5, Ti - 0, 08, Zr	

^{*} A special porous insulator developed by Battelle Memorial Institute, Columbus. Ohio.

The fundamental characteristics required in emitter and collector materials are: general thermal resistance and mechanical integrity, good electrical conductivity and low thermionic work functions. Of these three, experiments showed the last two to be the least important because little could be done to preserve and accumtegrity in the highly reactive atmosphere of a dissociated-ionized air. Most retractory metals formed high resistance oxide layers on the collector and lost power output after 15 seconds of run time. This was not the case with S-30 models with $1800-2000^{\circ}$ C surface temperatures where oxides become collected. Phenolic impregnated with graphite had higher electric resistance than pure graphite and gave 70 percent of the output obtained from graphite models (see "Optimum Results" below). The best output was obtained in a graphite (emitter) - TZM (collector) model primarily because of good collector-to-sting contact and volatile oxides. Pyrolitic graphite emitters produced a uniform emission but the a-direction conductivity offered resistance as high as phenolic carbon.

The insulators were chosen primarily for good thermal shock properties. Of these BMI-785 ranked best, followed by boron mitride and M_2O_3 + 5 percent molybdenum dispersion. The porous nature of the first made it difficult to keep close mechanical tolerances and hence the last two were used most extensively.

D. Optimum Results

Data reduction showed blunted cone emitters (0, 25-inch emitter radius) followed by 6 - 10^{9} conical steerbods, $\beta < 0$, 15, and graphite or tungsten surfaces to yield the highest output (Figures 15 and 16). Figures 15-18 represent samples of outputs graphically. The solid lines are curve fits using Equation 1 with $\beta = 0$, 1, γ (argon) = 1,293, γ (air) = 1,155 and $\delta = 0$,05 to 1,0.

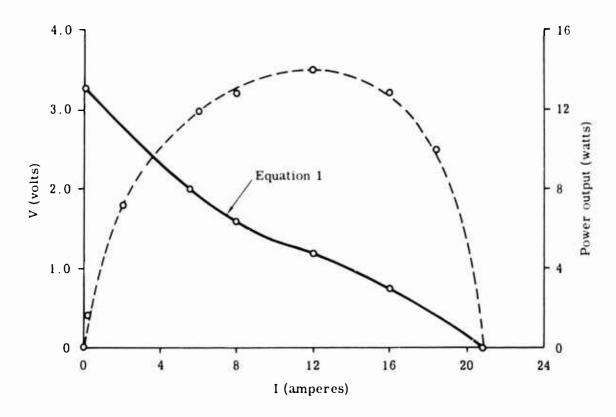


Figure 15. Output Data for β = 0, 15, V_T = 1 ev, δ = 0, 1 from S-6 Tungsten Model in Argon at 5000 BTU/lb

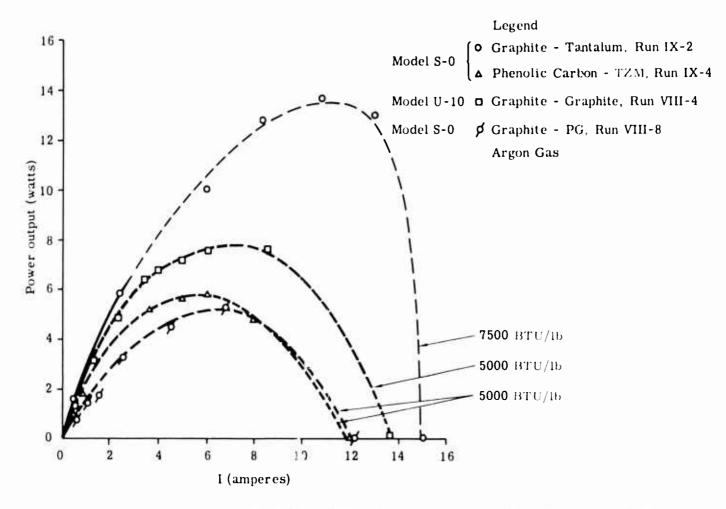


Figure 16. Power Levels from Various Models Showing the Effect of Argon Gas Energy on Output

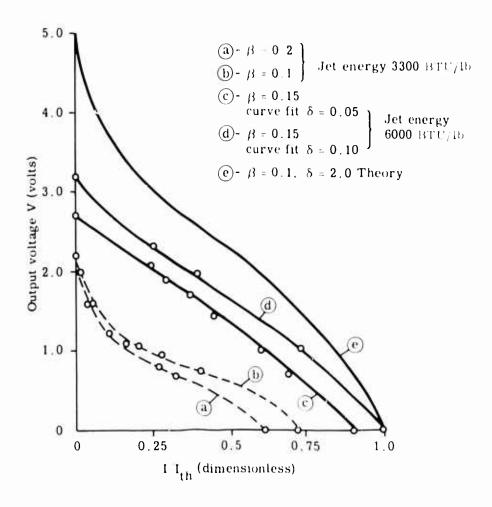


Figure 17. Voltage-Current Characteristics for V_T - 1.0. Various β and δ Values in Argon Gas

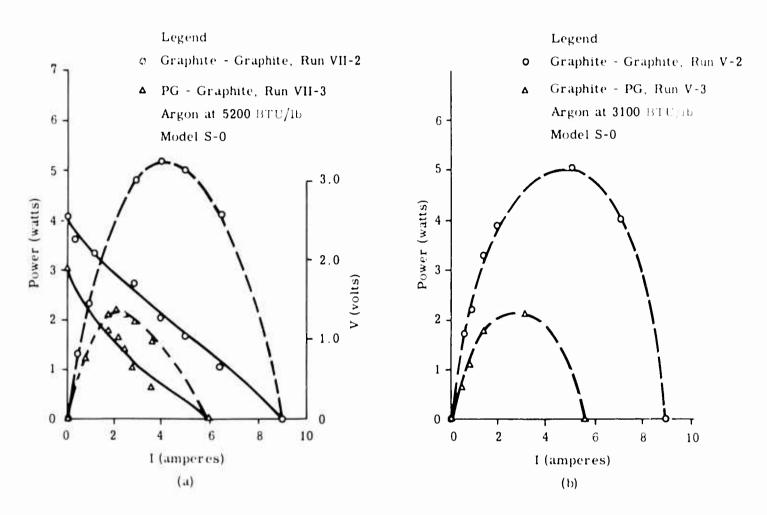


Figure 18.—Effect of Contact Resistance between Pyrolitic Graphite Shell and Carbon Substrate on Output

To estimate the maximum power output of this generator the expression Γ^{\prime} $\Gamma_{\rm th}$ (E. - $\Gamma_{\rm p}$

$$E \equiv V \leftarrow_{i} R$$

$$= I - I - I_{th}$$

Similarized (see Reference 1) and plotted as a function δ (thermionic to random electron ratio) for various table—of β and r (or r) in Figure 19. For plasma densities encountered in a plasma jet $\delta \approx 0.1$. The effect of r on β is seen to increase as β decreases (or as the collector size increases). (See also Figure 14.) there is not enough reliable data for r to allow a direct experimental check of Figure 19. The trends, however, are in the expected direction as observed in Figures 13-19, and especially in Figure 18 where β is an "effective" value, taking into account r and r.

Maximum short-circuit current measured was 24 amps over a hemispheric emitter R = 378 m at 3250 K. According to the Richardson-Dushman equation

$$I_{\text{th}} = C^{\dagger}A_{\text{em}}^{\dagger}T^{2} \exp\left(-\frac{e\phi_{\text{e}}/kT_{\text{em}}}{}\right)$$

this should yield $t_{\rm th}=78$ for C1 = 120. However, if one assumes $T_{\rm em}$ to be a function of θ , the azimuthal angle, and assumes a parabolic temperature drop from stagnation point $\theta=0$ to $\theta=\pi/2$ or $T_{\rm em}=3250-200$ θ^2 , the above equation yields

$$I_{\text{th}} = 240 \ \pi R^2 \int_{\Theta} T_{\text{em}}^2 (\theta) \exp \left[-\frac{e\emptyset}{kT_{\text{em}}(\theta)} \right] \sin \theta \, d\theta$$

or 1 = 27 amps. Table VII summarizes the optimum output per emitter area with several different materials both in argon and in air.

TABLE VII

Optimum Output per Emitter Area

		Argon (5,000 BTU/lb)			$\Delta m (12,000 \ B10 \ 1b)$		
Model	Material	$\frac{1}{sc}$	\oc\olts	Maximum Power watts_in ²	lsc amp_in_2	\ \olts	Maximum Power witts in
$\frac{S-6}{(12^{\Theta} \text{ blunted cone})}$ $\frac{B+0}{3}$	Graphite (emitter, collector)	21	3, 25	15	4, 0	1. 3	2. (
	Phenolic carbon emitter, graphite collector	15	3, 25	8	3. 0	1. 0	1, 5
S-30 ⁰ HRV Shape	Tungsten (emitter, collector)	21	3.0	7	4 5	1, 7	2.3
$\beta = 1/2$	Phenolic carbon (emitter, collector)				3 8	1, 4	1, 4

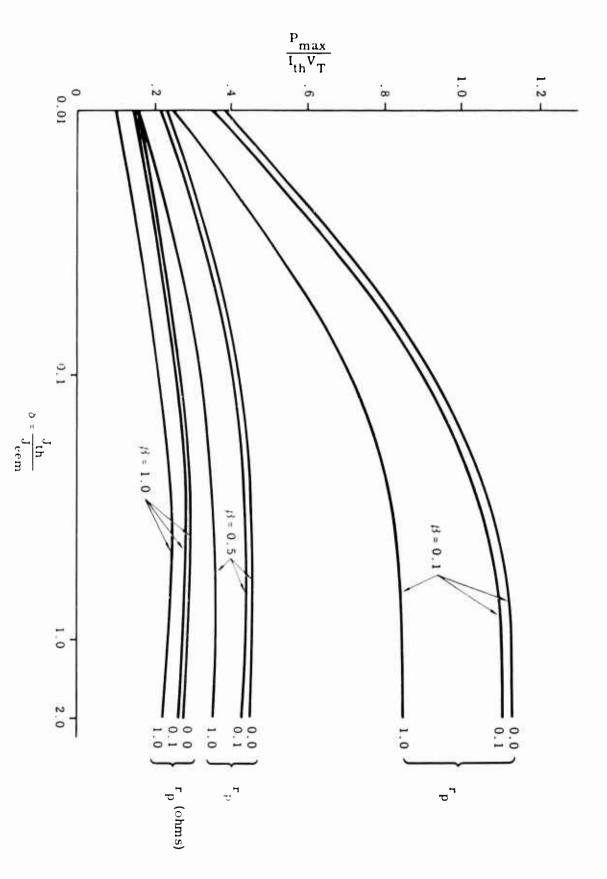


Figure 19. Dimensionless Maximum Power versus for Various Values of A and r

I we things are obvious from Table VII. Thirst phenomic carbon is seen to over go about 70 percent of the short care at current of graphite and 60 percent of the power output with no signalicant change in specifical coating. The former two show the effect of $m_0 = 1$ impedance offered by the material and the latter points to the fact that V_{int} depends primited von the piesmicenergy. Second, comparing the s-6 shape with B = 0, I to the S-30 sharp cone model with B = 1, at is easy to see how a large collector-to-emitter are exampled (small P) affects output in the case of argon. However, this ratio is more than compensated for incern because of considerably lower plasmic conductivity of the factor.

The highest short circuit current recorded to date in argon was 28 amps an ² of emitter area and the highest open-circuit voltage. 4.4 volts. In air, these values were 8 amp an ² and 2.3 volts, respectively. Repetability of runs for identical models were governed charity by reliability of consecutive runs in the plasma jet and repetability of contact resistance. Under best conditions of control repetability varied between 10 and 25 percent. When contact resistance was under close control, low are jet reliability was caused primarily by electrode crossion.

Free Flight Conditions

It is difficult to assess the exact range of applicability of plasma jet experiments to free flight conditions where the air is shock ionized and has comparatively lower kinetic temperatures than those found in an arc jet. Figure 20 is a plot of electron temperatures and degree of ionization over a remen diameter blunt hemisphere exhiber on a recentry trajectory with 22, 507 ft see recentry velocity. Between altitudes of 250 to 100 kilotect ephenolic carbon emitter can be made to vield a maximum of 150 amps short circuit current with 2-0 volts open-circuit voltage (75 waits) by directly scaling-up the plasma jet data obtained in air. According to Figure 21, however, electron conductivities in the boundary layer are not expected to exceed 100 mbo cm. The plasma resistance over an effective electron path of 5 mehrs will then be at least 0, 1 ohm, reducing the vehicle output to 20 waits. This will require increasing the voltage output to drave the large the ringer a contents by either dividing the surface into several emitter-collector pairs or using supersate dite accentry speeds generating 6-10 volts open-circuit voltage. Fifther of these methods will cause the output of a full-size recentry vehicle (3, 0-ft disenseter) to be 1 km or more. Because of high recombination rates, no output deexpected below 30,000 feet distade unless some form of seeding is used from the assessor. Furthermore, high pressure rear the stagnation point is expected to inhabit the resort combination for the total R (4 - mean free path at center wall).

Lature Work

Some of the results reported here are not vet final. A set of plasma tests in a larger (2.25-inch diameter) jet are expected to yield more reliable results on the combined effects of increasing collector and emitter are is and thereby lengthening average electron paths from emitter to collector but still holding contact resistance to a minimum. From trends obtained to date it is expected that increased values of r_p will slowly decrease the l_{th} versus A_p curves (Figure 8).

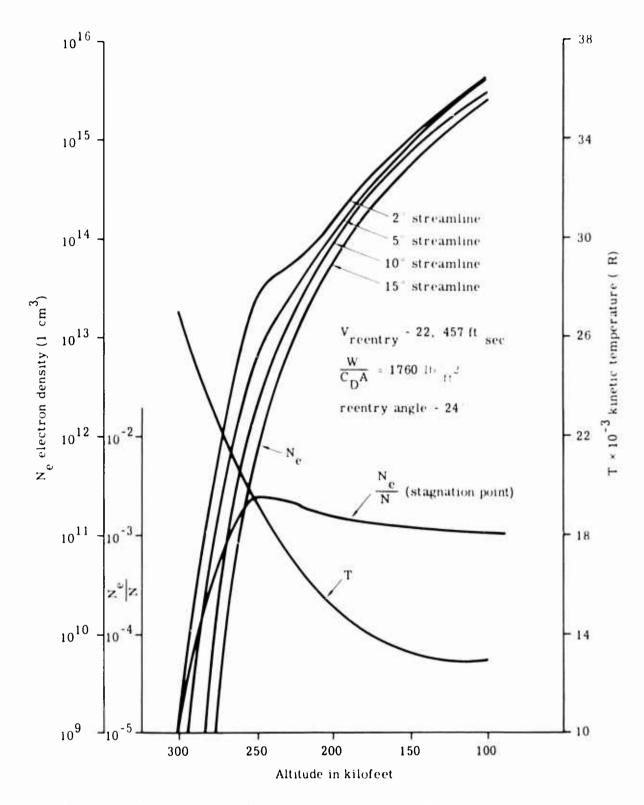


Figure 20. Electron Density and Kinetic Temperature Near Stagnation Point for Blunt Re-entry Vehicle at Various Altitudes

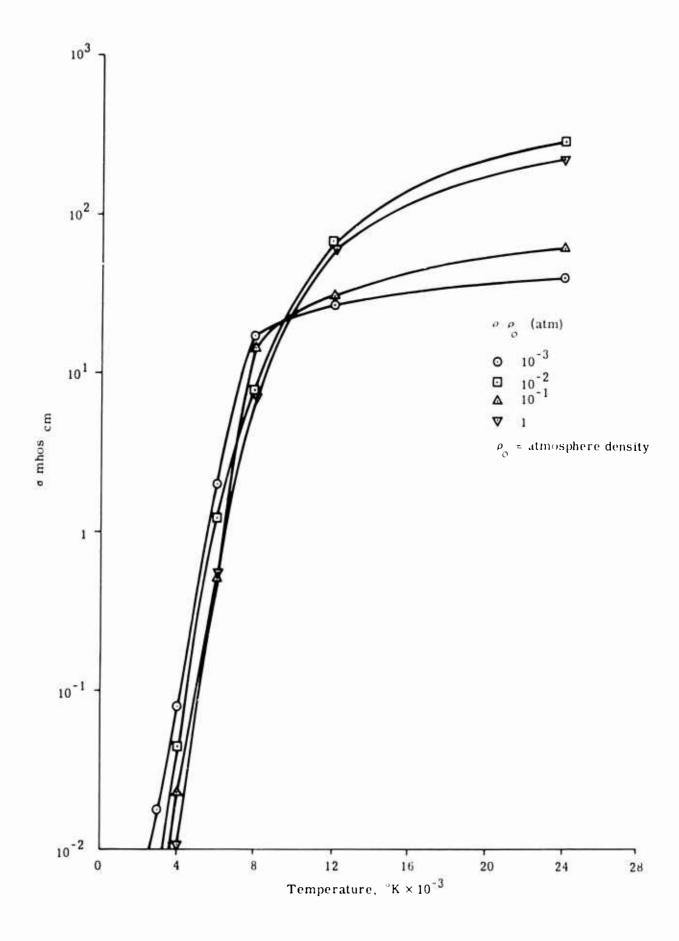


Figure 21. Electrical Conductivity as a Function of Temperature for Equilibrium Air at Various Densities (Liquation B-5)

Several runs will also be made with desium impregnated tungsten emitters to simulate in-flight seeding conditions, and a new set of heat resistant carbide surfaces will be tested. Finally, models have been designed with two emitter-collector pairs to evaluate the "in-series" behavior of such a generator. These results will be given in a separate report before the end of the year.

APPENDIX

Three analytical points will be discussed briefly in this Appendix: the sheath potentials at the emitter and collector, the effect of joule heating and Thompson emit in the plasma generated by the large currents dumped into it from emitted electrons, and high density plasma sheaths with mass velocity.

$$\lambda$$
. Note on V_{em} and V_{e}

In Reference 1. Equation 3 for the current flow at the emitter is written as

$$1*1_{th}*1_{tem}*1_{tem}=\exp\left(*\frac{e|V|}{k}\frac{em}{T_{e1}}\right)$$
 for negative V_{em} (zero plasma potential) (\forall -1)

⊒Eid

$$1 - I_{th} \exp\left(-\frac{e V}{k T_{em}}\right) - I_{eem} \text{ for positive } V_{em}$$
 (A-2)

From Equation V-1, solving for Vem

$$V_{em} = \frac{\frac{k}{c} T_{e1}}{e} I_n \left[\frac{\frac{l_{eem}}{l_{th} + l_{tem} - 1}}{\frac{l_{em}}{l_{th} + l_{tem} - 1}} \sqrt{\frac{k}{2} \frac{r_{e1}}{r_{e}}} \right]$$

$$= \frac{\frac{k}{c} T_{e1}}{e} I_n \left[\frac{\frac{l_{eem}}{l_{th} + l_{tem} - 1}}{\frac{l_{em}}{l_{th} + l_{tem} - 1}} \sqrt{\frac{k}{2} \frac{r_{e1}}{r_{e}}} \right]$$
(A-3)

Similarly at the collector, for $V_{\overline{\varepsilon}} < \sigma$

$$V_{c} = \frac{k T_{e2}}{e} \ln \left[\frac{n_{e2}e}{J + J_{1e}} \sqrt{\frac{k T_{e2}}{2 \pi m_{e}}} \right]$$
 (A-4)

Taking into account the resistive drop in the cell, the net voltage of the generator becomes

$$V = V_{\text{cm}} + V_{\text{c}} + \emptyset_{\text{c}} - \emptyset_{\text{c}} - \text{IR}$$
 (A-5)

It is also from this equation that for $\psi_c = \psi_c = 0$, the barrier potentials at the cathode and the anode are of the gramportance. Tooking at Equations A-3 and A-4 above, it becomes obvious that for $T_{c2} \leq T_{c1}$, $V_c \leq 1$ decrease at least proportionally to a decrease in T_{c1} . Actually, the decrease in V_c is proportional to $T_{c2} \approx 1$ for J=0 for example, $T_{c2} = 9000^{\circ} \text{K}$ ($T_{c2} = 12,000^{\circ} \text{K}$) in argon, $V_c = 0.57$ V_c

The equivalent expression to Equation 1, with $T_{e1} \ge T_{e2}$ is

$$V = V \prod_{\Gamma} \frac{\left[\frac{1 + \gamma/\delta - 1}{\gamma/\delta\beta + 1}\right]^{1/\Gamma} \Gamma}{\left[\frac{1 + \gamma/\delta - 1}{\gamma/\delta\beta + 1}\right]} + \emptyset_{c} - \emptyset_{c} - 1R$$
(A-6)

where $T_1 = T_{e1} T_{e2}$, and subscript 1 and 2 refer to plasma conditions at emitter and collector respectively.

B. Thermoelectric Effects in a Joule-Heated Plasma

N. Rynn (Reference 8) and L. S. Hall (Reference 9) have analyzed the thermoelectric effects in fully somized joule heated plasmas. It is a straightforward method to extend the analysis to the case of partially somized gases. Assume $n_1 = n_2 = n$ and n_1 neutrals. Neglecting inertia terms the equation of motion for electrons; according to Cowling (Reference 10), leads to,

$$0 = -\nabla p_{c} - neE - nm_{c} \sqrt{\tau^{-1}} - nm_{c} \left\{ \sqrt{\tau} + \sqrt{\tau} \left(1 + n/n_{c} \right) \right\} \tau_{c}^{-1}$$
(B-1)

and for ions

$$(1 - f) \rho \frac{dv^{\dagger}}{dt} = -\nabla p_{1} + neE - \frac{m_{e}}{\tau_{e}} j^{*} - \frac{m_{1}}{2e\tau_{1}} j_{1}^{*} f^{-1}$$
(B-2)

where

$$\overline{f}^{-1} = 1 + n/n$$

$$j - \text{nev}, j - \text{nev}$$

ver the velocity of the mass as a whole

time between successive collisions

The rest of the notation is conventional,

Adding Equations B-1 and B-2,

$$f_{\nabla P_{\underline{e}}} = \frac{m_{\underline{e}}}{\underline{e} \, \underline{\tau}} \, \underline{j} + \underline{j}_{\underline{i}} \, f^{-1} \left[\frac{m_{\underline{e}}}{\underline{e} \, \underline{\tau}} + \frac{m_{\underline{i}}}{2 \, \underline{e} \, \underline{\tau}_{\underline{i}}} \right].$$

substituting for \underline{j}_{1} in the electron equation, yields

$$\operatorname{ne} \widetilde{E} + \begin{bmatrix} \frac{m}{e} \\ 1 - f \frac{\frac{m}{e\tau}}{\frac{e}{e\tau} + \frac{1}{2e\tau}} \end{bmatrix} \nabla p_{e} = \begin{bmatrix} \frac{m}{e\tau} & \frac{mm}{1-e\tau} \\ \frac{1}{e\tau} & \frac{1}{e\tau} & \frac{e}{e\tau} \\ \frac{e}{e\tau} & \frac{1}{e\tau} & \frac{1}{2e\tau} \\ \frac{e}{e\tau} & \frac{1}{e\tau} & \frac{1}{2e\tau} \end{bmatrix} ;$$
(B-3)

For $m_0, m_1 < \epsilon$ 1 Equation B-3 simplifies to

$$neE + \nabla p_e = \frac{m_e}{e\tau} \hat{j}$$
 (B-4)

From here on we follow Rynn (Reference 8) and write the current and energy equations for one dimensional motion

$$\begin{vmatrix}
J = -\sigma E + b\sigma \frac{d\theta}{dx} \\
Q = \epsilon \sigma \theta E - d\sigma \theta \frac{d\theta}{dx}
\end{vmatrix}$$

$$\frac{dQ}{dx} = -JE + \frac{5}{2}J \frac{d\theta}{dx}$$
(B-5)

where $\theta = \frac{kT}{c}$ and the rest of the terms are identical to those of Reference 8, except for the (dditional term on the right of the third equation. Integrating this equation and setting $\phi = 0$, $\theta = \theta_0 \left(E = \frac{ds}{dx}\right) \frac{d\theta}{dx} = 0$,

$$Q = -j(\emptyset + \theta_{O}c^{\dagger} - f\theta)$$

$$= -j(4 - f\theta) \qquad f = \frac{5}{2}$$

Substituting these values in the first two equations of B-5 and introducing the new variable $\eta = \psi_i \theta$, the following equation is obtained

$$\frac{d\theta}{\theta} + \frac{c - (\eta - f)}{\eta(\eta - f) - [c\eta + b(\eta - f)] + d} d\eta$$
(B-6)

Equation 8-6 differs from that of Rynn only $^\circ$ the additional constant $t\to 2$. The collition of this equation is given as a quadrature in References 8 and 9 where the thermoelectric effects are shown to skew the electron temperature distribution towards the cathode. Lewis and Reitz (Reference 11) calculate the more ise in electron temperature by joule heating and for 50 amp cm² current levels, 0,06 mm Hg electron pressures and 6000° K initial temperature, obtain a value of $T_{\rm e} = 6000^{\circ}$ K. For $T_{\rm e} = 5$ amp cm² encountered in the present ASP generators, the rise of these emitter electron temperatures is not more than a few hundred degrees, and for are jet plasma temperatures, $T_{\rm e} = 12,000^{\circ}$ K, it is negligible and actually is camouflaged by collisions with the energetic plasma electrons.

C. High Density Plasma Sheaths with Mass Motion

With gas densities up to 0.1 atmosphere, neutral gas atoms mean free paths $\lambda \leftarrow R$. (R model body dimension) and mass velocities $v \approx 15,000$ ft/sec, it is imperative for one to take a more careful look at the plasma barriers and ion arrival rates with increased mass velocities, $v_{ij} = v$ at the electrodes ($v_{ij} = v = 0$). In collisionless plasmas, an initial velocity of 600 – t/sec in the ions (see Reference 1, Equation B-11) will cause v = 25 percent reduction in electron emission. However, in diffusion controlled plasmas, such a direct estimate is difficult to make and an entirely different approach is necessary. Only a general ordine will be given here, with details left for a future work.

The governing equations of motion for ion and electron diffusion in a slightly ionized g is of known flow characteristics are

$$\mathbf{d} \cdot \boldsymbol{\Delta} \mathbf{u}^{T} + \boldsymbol{\Delta} \cdot \boldsymbol{L}^{T} = 0 \tag{C-1}$$

where

$$\Gamma_{\mathbf{i}} = -D_{\mathbf{i}} \nabla n_{\mathbf{i}} - e Z \mu_{\mathbf{i}} n_{\mathbf{i}} \nabla \emptyset$$

$$\Gamma_{\mathbf{e}} = -D_{\mathbf{e}} \nabla n_{\mathbf{e}} + e \mu_{\mathbf{e}} n_{\mathbf{e}} \nabla \emptyset$$

and Poisson's equation

$$\nabla^2 \phi = -4\pi e \left(Z \mathbf{n}_1 + \mathbf{n}_2 \right) \tag{3.2}$$

where D - diffusion coefficient, μ - mobility, \emptyset - potential

Following the notations of Lamb (Reference 12), these three equations can be nondimensionalized to yield

$$a^{2} \nabla^{2} \psi = N_{1} + N_{0}$$

$$R(\nabla + \nabla N_{1}) + \nabla + \gamma_{1} = 0 \qquad (6.3)$$

$$\frac{1}{4D_c} \operatorname{R}(1 + \nabla \Sigma_c) + \nabla + \gamma_c = 0$$

where

$$R = \frac{LU}{D_1} = \frac{1}{\sqrt{2T_e}}, N_{e,1} = n_{e,1} n_{e,1}, \psi = -e \theta \cdot kT_e$$

$$e = h, E, h, Debve length$$

The analysis is then divided into two regions. The ambipolar diffusion region and the sheath region with matching boundary conditions at the interface. The sheath solution leads to the third order nonlinear equation

$$\epsilon \frac{d^{\frac{3}{3}}}{dt^{\frac{3}{3}}} = (\epsilon - 1) \frac{d\psi}{dt} \frac{d^{2}\psi}{dt^{\frac{2}{3}}} + \frac{1}{2} \frac{d\psi}{dt} \left[\left(\frac{d\psi}{dt} \right)^{2} + 2(1 + \epsilon)t \right] - (1 + \epsilon) \times$$
(C-4)

where tas sheath coordinate, proportional to the normal coordinate to the surface, and $X \sim (n \cdot \nabla \psi_{\beta}) \| \sqrt{R}$ is determined from the diffusion solution.

For $T_{\epsilon} = \Gamma_{1}$, $\epsilon = 1$, Equation C-4 simplifies to

$$\frac{\frac{d}{dt}\dot{\phi}}{3} = \frac{1}{2}\frac{d\phi}{dt}\left[\left(\frac{d\phi}{dt}\right)^{2} + 4t\right] - 2\chi \tag{C-5}$$

subject to boundary conditions

$$\frac{\mathrm{d}^2 \varphi}{\mathrm{d} t^2} = \mathbf{I}_{th} \, F(\varphi)$$

ALESSED FIGURES a function of the potential distribution in the sheath determined from interaction (collision)

Detweet the emitted electrons and the plasma electrons

$$\left(\frac{\mathrm{d}\dot{u}}{\mathrm{dt}}\right)^2 = -4t_{\Omega} + 2T_{\mathrm{th}} \mathrm{F}(\dot{u})$$

1,11

$$\frac{\mathrm{d}\psi}{\mathrm{d}t} \ (t - \epsilon) \equiv \sqrt{|t|}$$

For a floating potential, $\emptyset = \emptyset = \emptyset$, from Equation C-1 and C-2 one can show that $\begin{bmatrix} 1 & 4 & 6 & 3 & 4 & 4 & 1 \\ 4 & 4 & 1 & 4 & 4 & 1 & 4 & 1 \end{bmatrix}$ or, the ion is included and consequently electron emission is reduced by a factor of the knudsen number at the wall. A more relastic situation for ASP would be to consider a collision dominated ambipolar region and a free fall sheath region, with boundary condition (a) replaced by

$$\frac{\mathrm{d}^2 \dot{\psi}}{\mathrm{d}t^2} = I_{\text{th}} \exp\left(\psi \, \boldsymbol{\delta}\right) \left\{ 1 + \mathrm{err} \, \nabla \psi \, \boldsymbol{\delta}\right) \right\}, \; \boldsymbol{\delta} = T_{\mathrm{e}} \cdot T_{\mathrm{em}}$$

Analyses along these lines are presently under way, and results will be forthcoming in a separate report

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